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## Methodology for Micro-Insurance Introduction and Recent Advances

8<sup>th</sup> International Microinsurance Conference  
Dar es Salaam, November 6-8, 2012

Center for the Economic Analysis of Risk  
Dean's Behavioral Economics Laboratory





# Overview of Pre-Conference

- > Methodologies useful for evaluating micro insurance at the individual level
  - Behavioral economics
    - Insurance and risk management
    - Risk attitudes
    - Risk perception
  - Behavioral econometrics
  - Impact assessment, Randomized Controlled Trials, and Controlled Economics Experiments



# Schedule and People

- > **Elisabet Rutstrom, Georgia State University**
  - Experiments to evaluate risk attitudes and risk perceptions
  - Methodologies for assessing impact heterogeneity
- > **Jimmy Martinez, Copenhagen Business School**
  - Optimal Risk-Sharing Contracts: A Behavioral Perspective
  - Understanding the behavioral and institutional reasons for low demand
- > **Daniel Clark, Oxford University**
  - Theory and Experiments on Index Insurance



# Common Themes

- > Individual behavior
- > Economics experiments as data generation process
  - Theory driven design
    - Internal validity
  - Monetary, salient incentives
- > State of the art estimation techniques



# Inferential objectives

- > Impact analysis of policies, products and interventions at individual consumer level
  - Heterogeneity
    - Participation, success, winners and losers
  - Welfare effects relying on individual utility
- > Designing and testing normative policies, products and interventions



# Range of applications

- > Insurance demand
- > Self insurance
- > Self protection
- > Portfolio choice
- > Search behavior and information about risk
- > Updating risk perceptions and learning
- > Traded and non-traded risks

Elisabet Rutstrom

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Introduction

Methodology for Micro-Insurance

Controlled Randomized Experimentation

Dean's Behavioral Economics Laboratory





# What am I going to talk about?

- > Individual Behavior under Risk and Uncertainty
  - Demand for insurance or risk management
  - Heterogeneity due to attitudes and perception to risk
- > Generating behavioral data using economics experiments
  - Careful control for auxiliary influences on behavior
  - Theory guided design
  - Salient and real incentives
- > Analysing experimental data
  - Consistent with theory and experimental design





# For whom is this talk useful?

- > If you want to ...
- > Know When To Use Experimental Economics:
  - Quantitative measure of preferences under risk and uncertainty or for delayed rewards
  - risk attitudes, optimism/pessimism, regret, uncertainty/ambiguity preferences, time preferences and discount rates
- > Estimate demand for insurance products
  - Test marketing plus preference elicitation
  - Augmented Randomized Controlled Trials
- > Understand impact heterogeneity from risk management and insurance interventions
  - Heterogeneity in responses linked to heterogeneity in preferences



# LESSON ONE: Start with Theory

- > Before designing your experiment
- > Three elements in the theory:
  - Choices, preferences and perceptions
- > The simplest choice theories:
  - Expected value and Expected utility
- > Complicating the theory:
  - Stochastic choice, behavioral errors and sampling errors
  - Non-expected utility



# Example: Wild Fires

- > A risky, uninsured event
- > A wild fire will burn your property with some probability,  $\pi$ 
  - The property does not burn with probability  $(1 - \pi)$
  - Property value is  $W$
  - Fire damage is  $Z$
- > Expected value of uninsured event:
  - $\pi(W - Z) + (1 - \pi)W$



# Adding wild fire insurance

> Expected Value under Full insurance

>  $\pi(W - p_f) + (1 - \pi)(W - p_f) = W - p_f$

○  $p_f$  premium for full insurance

> Expected Value under insurance with deductible

>  $\pi(W - p_p - d) + (1 - \pi)(W - p_p)$

○  $p_p$  premium partial insurance

○  $d$  deductible



# Insurance choice under Subjective Expected Utility

- >  $\max\{\pi U(W - Z) + (1 - \pi)U(W)\},$
- >  $[\pi U(W - p_p - d) + (1 - \pi)U(W - p_p)],$
- >  $[U(W - p_f)]\}$
- > Maximum depends on properties of both  $U$  and  $\pi$  (subjective probability)
- >  $\pi$  is not the actuarial probability but the subjective probability “in the head of” the agent



# Demand for insurance



- > Each agent's demand for *full insurance* is
  - Decreasing in  $p_f$
  - Increasing in  $p_p, \pi, Z$
- > Each agent's demand for *partial insurance* is
  - Decreasing in  $p_p$
  - Increasing in  $p_f, \pi, Z$
- > *Concavity of U*
  - increases overall demand for insurance,
  - decreases relative demand for partial over full insurance



# Understanding heterogeneity in demand responses

- > Understanding heterogeneity in  $\pi$  and in concavity of  $U()$
- > Various structural versions of  $U()$
- > *One parameter CRRA*  $\frac{y^{1-r}}{1-r}$
- > *One parameter CARA*  $1 - e^{-\rho y}$
- > *Two parameter Expo-Power*  $\frac{1 - e^{-\alpha y^{1-r}}}{\alpha}$



# Estimating heterogeneity in demand based on behavioral parameters

- > Design an experiment to generate the data
- > Estimate utility parameters  $(r, \rho, (\alpha, r))$
- > Estimate subjective probabilities  $\pi$
- > Design an experiment that controls for *auxiliary behavioral influences*
  - Influences not captured by theory
  - Experimenter demand effects, cognitive difficulties, boredom





# Starting with theory will

- > Tell you which variables are influence variables and how they interact
- > Tell you how you need to focus on identification of these variables




# Designing the experiment

- > Implement a choice situation:
  - Example: Pairwise choice between partial insurance and non-insurance options
- > Specify a utility function:
  - Example: CRRA utility function
- > Estimate  $r$  and  $\pi$
- > Control variations in non-behavioral variables  $W, Z, p_p, d$ 
  - These vary with the product or intervention motivating study
- > In field data several of these variables may vary in unobserved ways
- > These can be controlled in an experiment



## LESSON 2: You cannot implement an ideal experiment

- > There are many ways to design a “near ideal” experiment
- > Let us review some problems that the experimenter will encounter when designing an experiment



# Why can't we just ask people what they would do?

- > Observations we make would be statements about intentions and not actions
- > What is the distinction between Statements, Intentions and Actions?
- > Ideally we want to observe Actions
- > Do Statements predict Actions?
- > Possible that Statements  $\neq$  Intentions = Actions
  - No truth-telling incentives
- > Possible that Statements = Intentions  $\neq$  Actions
  - Subject's do not accurately predict actions



# Truth telling

- > Even when respondents know their preferences they may not make statements that reflect them
- > Strategic reasons
- > Cognitive cost reasons
- > Provide incentives to tell the truth
- > Observing action choices in the presence of incentives



# Poor self predictions

- > Even when using truth telling incentives
- > Respondents may be unfamiliar with the situation or environment
  - They have no experience in the issue and don't know what they would do
  - They predict their own actions with some error, perhaps even biases



# Problems with auxiliary influences

- > Theory is simple and focuses on core variables
- > Real life is never simple, and real decisions are always influenced by a wide variety of factors, even in controlled lab environment
- > Experimenter demand effects
  - Wanting to please the experimenter
- > Cognitive fatigue or cognitive dysfunctions
- > Mood and emotions
- > Unfamiliarity with task and lack of attention to instructions
  - Learning and updating



# Example of possible auxiliary influence

- > Give subject a choice between two risky situations with monetary consequences
- > 1. No insurance case:  $W=\$50$ ,  $Z=\$40$ ,  $\pi = .25$ ,  $EV=\$40$
- > 2. Full insurance case:  $W=\$50$ ,  $p_p =\$12$ ,  $EV=\$38$
- > Risk neutral subject should choose No insurance
- > If he chooses insurance:
  - He is risk averse
  - OR something else outside of theory motivates his choice or interferes with his valuation





# Summary of Design Problems

- > Uncontrolled variation in influence variables  $W$ ,  $Z$ ,  $d$ ,  $p$
- > Lack of truth telling or ideal prediction circumstances
- > Uncontrolled variation in auxiliary influences



# An Ideal Experiment ...



- > Makes all influence variables ( $W$ ,  $Z$ ,  $p$ ,  $d$ ) observable
- > Implements a choice situation with actual consequences
- > Observes actions directly – no need to infer actions from statements of intentions
- > Removes auxiliary influences
  - Or uses randomized recruitment and assignment to treatment to randomize such influences
- > So that we can infer the behavioral parameters from the observed actions
- > And predict demand



# What to do?

- > Cannot achieve ideal experiment
- > But get as close as possible
- > Observe as much of auxiliary variables as possible
- > Randomize over other possible auxiliary influences



# A Popular Method: Randomized Controlled Trials (RCT)

- > Purpose is to test for significant effect of intervention or product:
  - Will the change in the fire insurance conditions increase demand?
  - Typically no estimation of behavioral parameters
  - Randomize to control for influences from behavioral heterogeneity and auxiliary influences -
- > Is randomization sufficient?
- > For very large samples
  - Variations in subjective probabilities are randomized across conditions
  - Utility function parameters are randomized across conditions
  - Auxiliary influences are randomized across conditions



# Economics Experiments as Alternatives to RCTs

## > Controlled economics experiment

- Includes the intervention conditions
- Includes elicitation of behavioral parameters
- Includes surveys or other experimental observations to capture auxiliary influences
  - Demographics, experimenter influences, environmental variables like time of day, learning and order of tasks, etc.

## > Randomize over unobservable auxiliary conditions



## Next

- > Once you understand the nature of these problems
- > And you know your theory
- > You can start designing the experiment
- > Choice of elicitation instruments should be guided by theory and your understanding of the presence of auxiliary influences
  - Whether you know what they are or not



# Eliciting Willingness to Pay for insurance

- > Willingness to pay instruments
  - Elicit demand
- > Demand depends on risk attitudes and perception of risk
- > Correcting for concavity of utility function
  - Risk attitudes
- > Inferring beliefs
  - Subjective probabilities



# Price List design (WTP)

## Partial Insurance Demand

Premium	YES	NO
0	$\pi U(W-d-0)+(1-\pi)U(W - 0)$	$\pi U(W-Z)+(1-\pi)U(W)$
0+x	$\pi U(W-d-x)+(1-\pi)U(W - x)$	$\pi U(W-Z)+(1-\pi)U(W)$
0+2x	$\pi U(W-d-2x)+(1-\pi)U(W - 2x)$	$\pi U(W-Z)+(1-\pi)U(W)$
0+3x	$\pi U(W-d-3x)+(1-\pi)U(W - 3x)$	$\pi U(W-Z)+(1-\pi)U(W)$
0+4x	$\pi U(W-d-4x)+(1-\pi)U(W - 4x)$	$\pi U(W-Z)+(1-\pi)U(W)$
0+5x	$\pi U(W-d-5x)+(1-\pi)U(W - 5x)$	$\pi U(W-Z)+(1-\pi)U(W)$
0+6x	$\pi U(W-d-6x)+(1-\pi)U(W - 6x)$	$\pi U(W-Z)+(1-\pi)U(W)$
0+7x	$\pi U(W-d-7x)+(1-\pi)U(W - 7x)$	$\pi U(W-Z)+(1-\pi)U(W)$
0+8x	$\pi U(W-d-8x)+(1-\pi)U(W - 8x)$	$\pi U(W-Z)+(1-\pi)U(W)$





# Heterogeneity

## > Heterogeneity in switch points

- Choice depends on both  $\pi$  and concavity of U
- Choice also depends on auxiliary influences

## > COMMON PROBLEM 1

## > Identification (avoiding overfitting)

- Estimate both  $r$  (curvature of U) and  $\pi$
- Requires independent variations in more than just the premium
  - Vary damages  $Z$  or deductible  $d$
- Or use separate tasks for identifying  $r$  and  $\pi$



# Numeric example of non-identification

- >  $W=\$30$ ,  $Z=\$25$ ,  $d=\$2$
- >  $p=\$1\dots\$15$
- > Observe a switch from Yes to insurance to No to insurance as  $p$  goes from  $\$4$  to  $\$5$
- > Explained by
- >  $\pi=.1$  and  $r=.8$
- > or
- >  $\pi=.2$  and  $r=.1$
- > Solution:
- > Estimate  $r=.8$  from some other task, then  $\pi=.1$



## Watch out for

- > Many experiments suffer from over-fitting and underidentification
- > Estimation then reflects
  - Sampling errors
  - Measurement errors
  - Auxiliary influences
- > Next: using separate tasks for each parameter to be estimated



# Add a separate risk attitude elicitation task

- > Choice between risky options with known probabilities
  - No need to estimate subjective probabilities
- > Choices reflect risk attitudes only
- > Price List Method again

P of high	Low Safe	High Safe	Low Risky	High Risky
.2	20	30	1	38.5
.4	20	30	1	38.5
.6	20	30	1	38.5
.8	20	30	1	38.5

P of high	Low Safe	High Safe	Low Risky	High Risky
.5	20	24	1	16
.5	20	28	1	31
.5	20	32	1	46
.5	20	36	1	61

Certain	P of high	Low Risky	High Risky
22	.5	1	16
24	.5	1	31
26	.5	1	46
28	.5	1	61

1. Varying probabilities for constant prizes

2. Varying prizes for constant probabilities

3. Certain option

So many options – how do I choose?

- Certainty bias
- Mistaken portfolios
- Focal points
- POWER



- > COMMON PROBLEM 2
- > Lack of power
- > The same choice may be generated by a wide range of risk coefficients



# Example of low power

Certain	P of high	Low	High	EV of Risky
10	.5	0	180	90
20	.5	0	160	80
30	.5	0	140	70
40	.5	0	120	60
50	.5	0	100	50
60	.5	0	80	40
70	.5	0	60	30
80	.5	0	40	20
90	.5	0	20	10
100	.5	0	0	0



# Identifying switch points for various $r$

Certain	$r=.05$	$r=.1$	$r=.2$	$r=.3$	$r=.4$	$r=.5$	$r=.6$	$r=.7$	$r=.8$	$r=.9$
0										
10										
20										
30										
40										
50										
60										
70	x	x	x	x	x	x	x	x	x	x
80										
90										
100										





# Identifying switch points for various $r$

Certain	$r=.05$	$r=.1$	$r=.2$	$r=.3$	$r=.4$	$r=.5$	$r=.6$	$r=.7$	$r=.8$	$r=.9$
0	x	x	x							
100				x						
200					x					
300						x				
400							x			
500								x		
600									x	x
700	x	x	x	x	x	x	x	x	x	x
800										
900										
1000										



# LESSON 3: Details of instruments matter

- > Parameter variation and power
- > Price list:
  - Random incentive lottery mechanism (RILM)
  - switching back and forth
- > Multiple tasks, one at a time
  - Order effects
  - RILM
- > One task:
  - Learning and sample size
- > Pay all:
  - Control for wealth effect



# Inferring subjective beliefs – Econometric specification

- > We have elicited risk attitudes in lottery task
- > We have elicited switch points in the WTP task
- > We can now estimate a full decision model under EUT
- >  $EUT_{no\ ins}[\pi U(W - Z) + (1 - \pi)U(W)],$
- >  $EUT_{part\ ins}[\pi U(W - p_p - d) + (1 - \pi)U(W - p_p)],$
- > Choice rule:  $EUT_{part\ ins} > EUT_{no\ ins}$  then choose insurance



# Maximum Likelihood Estimation

- > Find the  $r$  and  $\pi$  combination for the two EUT choice models that maximizes the likelihood that our experimental observations (across both tasks Lottery and Price List) are generated by the theory process (EUT)
- >  $\max \prod_{i=1}^n f(x|(r, \pi))$
- > The function  $f(\cdot)$  is usually assumed to be cumulative normal, or logistic
- > LESSON 4: Theory needs to be augmented by a stochastic choice process

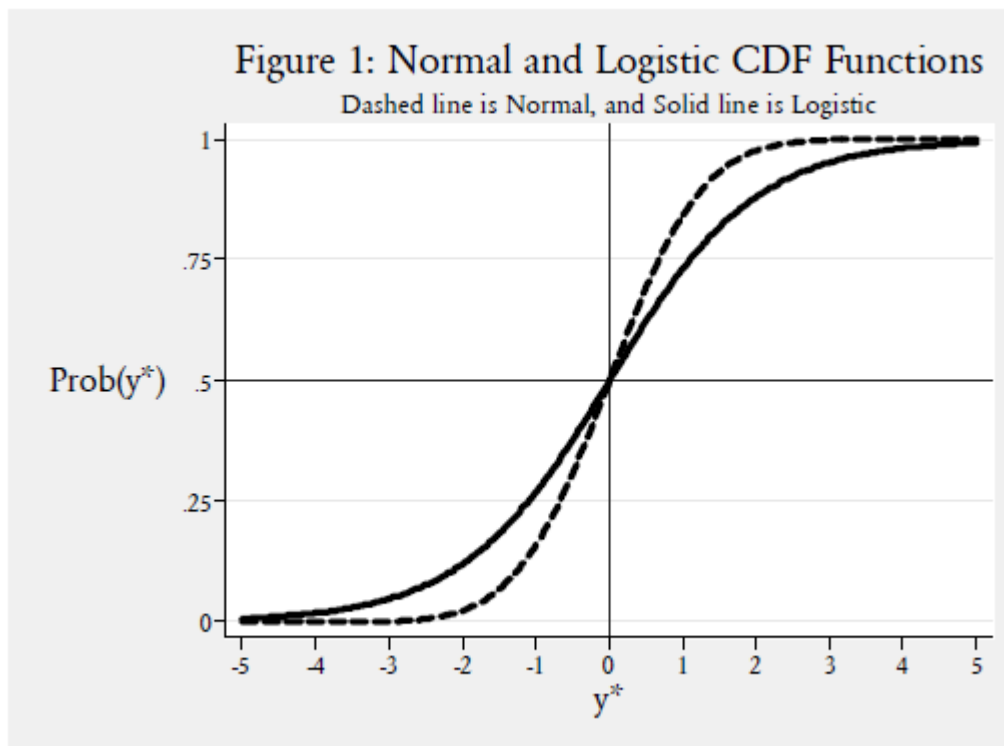


# Estimation steps

- > Specify the utility function
  - Example CRRA -  $r$
- > Specify SEU for each option NI (No Insurance) and PI (Partial Insurance) -  $\pi$
- > Specify index function for the choice propensity
- >  $\nabla SEU = SEU_{NI} - SEU_{PI}$
- > Stochastic choice of NI
- >  $P_{NI} = \phi \nabla SEU$
- > Select behavioral parameters to Maximize Log Likelihood that data is generated by this model

# Specifications

## > Adding behavioral errors – Fechner errors



For any given density function, Fechner error changes curvature  
Sensitivity to SEU differences

$$y^* = \nabla SEU$$



# Fechner errors

- > Adding Fechner errors to the index function:
- >  $\nabla SEU = \frac{1}{\mu} (SEU_{NI} - SEU_{PI})$
- > Adds one more parameter to be estimated
  - Need to worry about power again
- > Used to infer varying payoff sensitivities across tasks or subjects



# Non-EUT

- > Rank Dependent Utility
- > Introduces probability weighting
- > And violation of independence axiom (if more than two outcomes)
- >  $RDU_{no\ ins} [w(\pi)U(W - Z) + (1 - w(\pi))U(W)],$
- >  $EUT_{part\ ins} [w(\pi)U(W - p_p - d) + (1 - w(\pi))U(W - p_p)],$
- > Specifications of  $w(\pi)$





# Probability weighting specifications

> Simple one parameter power function

>  $w(\pi) = \pi^\gamma$

> One parameter Kahneman-Tversky function

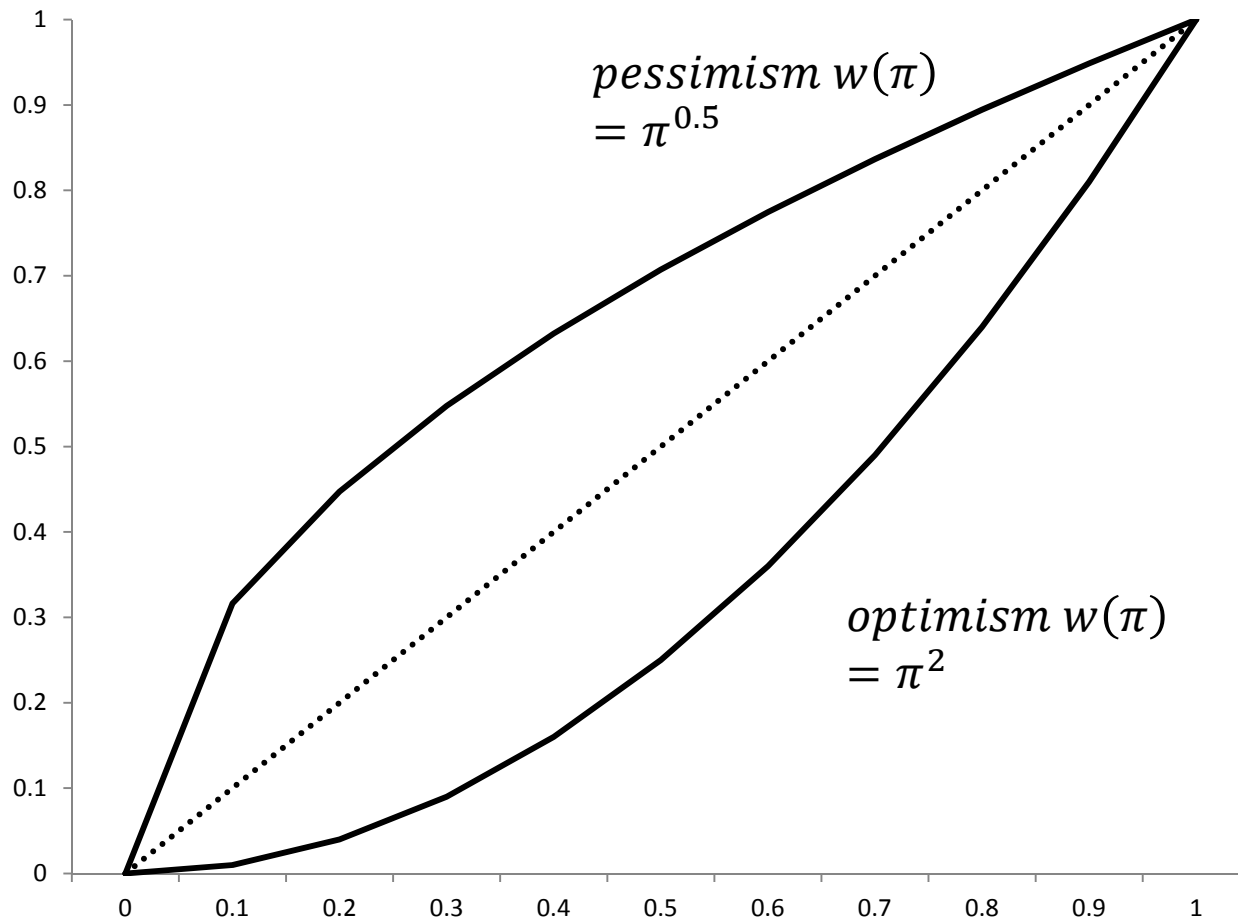
> 
$$w(\pi) = \frac{\pi_i^\gamma}{(\sum \pi_j^\gamma)^{\frac{1}{\gamma}}}$$

> Two parameter Prelec function

>  $w(\pi) = e^{-\delta(-\log(\pi))^\gamma}$

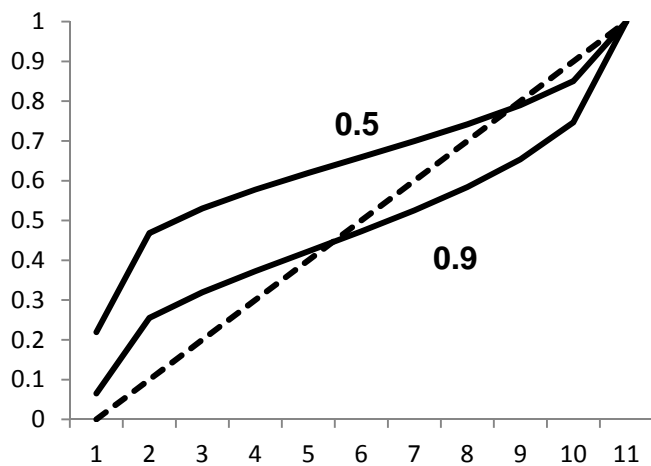


# Optimism and Pessimism Power Function

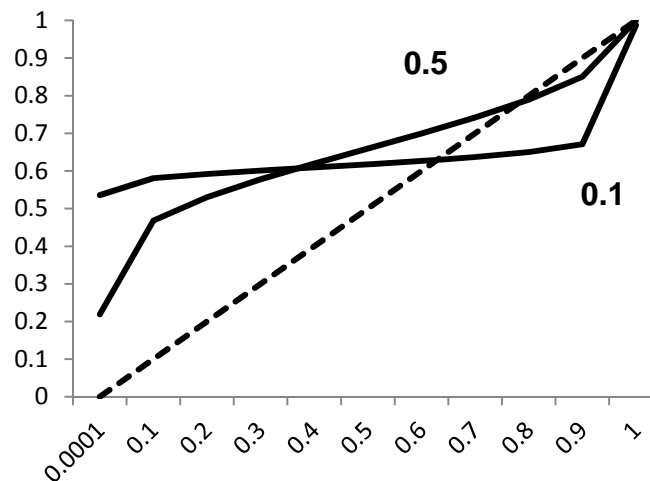




# Two parameter Prelec functions



Varying  $\delta$



Varying  $\gamma$



## LESSON 5: Identification quickly becomes a problem in flexible models

- > Require additional tasks with known probabilities
- > One task for each parameter
- > Recall each task is really a series of task identifying switching points
- > Cumulative Prospect Theory
  - Also add in loss aversion parameter
  - AND the often neglected reference point



# Parameter heterogeneity - findings

- > Introduce demographic covariates
- > Or estimate random coefficients
- > Some results from
- > Harrison, Glenn W., and Rutström, E. Elisabet, “Risk Aversion in the Laboratory,” in J.C. Cox and G.W. Harrison (eds.), *Risk Aversion in Experiments* (Bingley, UK: Emerald, Research in Experimental Economics, Volume 12, 2008).
- > Harrison, Glenn W., and Rutström, E. Elisabet, “Expected Utility And Prospect Theory: One Wedding and a Decent Funeral,” *Experimental Economics*, 12(2), 2009, 133-158.



# Heterogeneity in EUT estimation of risk attitudes

- > Student subjects, known probabilities
- > Homogeneous specification:
  - $r=0.229$  and  $\mu=.97$
  - Slightly concave utility, behavioral errors do not create large deviation from logistic cumulative density function
- > Heterogeneous specification using demographic covariates

	Point Estimate
r constant	0.754
Female	0.156
Black	0.100
Hispanic	0.232
Age in years	-0.030
Business major	0.025
Low GPS	-0.061
$\mu$ constant	1.235
Female	-0.246
Black	-0.022
Hispanic	-0.020
Age in years	-0.018
Business major	0.048
Low GPS	0.335

Very  
concave

Insensitive  
to EU  
differences



# General findings

- >  $r$  is generally between 0.2 and 0.8
- > Demographic effects vary across populations and type of tasks
- > Fechner errors are sensitive to tasks



# RDU and CPT one parameter KT probability weighting

	Point estimate
RDU $r$	.27
RDU $\gamma$	.99
RDU $\mu$	.94
CPT $r$	.42
CPT $\lambda$	.69
CPT $\gamma$	.93
CPT $\mu$	.74

Weak optimism

# RDU and CPT one parameter KT probability weighting

	Point estimate
RDU $r$	.27
RDU $\gamma$	.99
RDU $\mu$	.94
CPT $r$	.42
CPT $\lambda$	.69
CPT $\gamma$	.93
CPT $\mu$	.74

Less concave than EUT

# RDU and CPT one parameter KT probability weighting

	Point estimate
RDU $r$	.27
RDU $\gamma$	.99
RDU $\mu$	.94
CPT $r$	.42
CPT $\lambda$	.69
CPT $\gamma$	.93
CPT $\mu$	.74

Not loss averse



# General findings

- > Populations often mix of optimists, pessimists, s-shaped and inverse s-shaped probability weighting functions
- > Loss aversion sensitive to reference points
- > Fechner errors sensitive to specifications, tasks and subject pools



# Implications for impact analysis

- > Insurance demand
  - Heterogeneous utility functions but predominantly concave
  - Heterogeneous probability weighting functions
- > Increase in damages will increase insurance demand in most populations due to consistency in finding risk aversion
  - The magnitude of the effect varies
- > Increase in likelihood of risk will have an effect that depends on the probability weighting functions



# Implications from probability weighting

- > Increase in likelihood of risk will have an effect that depends on the probability weighting functions
  - Small risks with optimism means demand increase is deflated
    - Inverse S shaped have pessimism for small risks
  - Medium risks insensitive to changes if inverse S shaped
    - But frequently not inverse S shaped but concave
    - Or even S shaped so very sensitive to changes
  - Large risks demand increase inflated if inverse S shaped
  - Large risks demand increase inflated if optimism



# Subjective beliefs some findings

- > Eliciting subjective probabilities
- > Andersen, Fountain, Harrison, Risa Hole, and Rutstrom, Theory and Decision, 2010
- > In two outcome cases cannot identify subjective probabilities and probability weighting from same task
- > Example here based on SEU
- > Lab experiment using bingo cages with various proportions of orange and white pingpong balls
- > Betting mechanism for eliciting probabilities
- > Jointly eliciting risk attitudes using lottery tasks, controlling for  $r$



# No heterogeneity

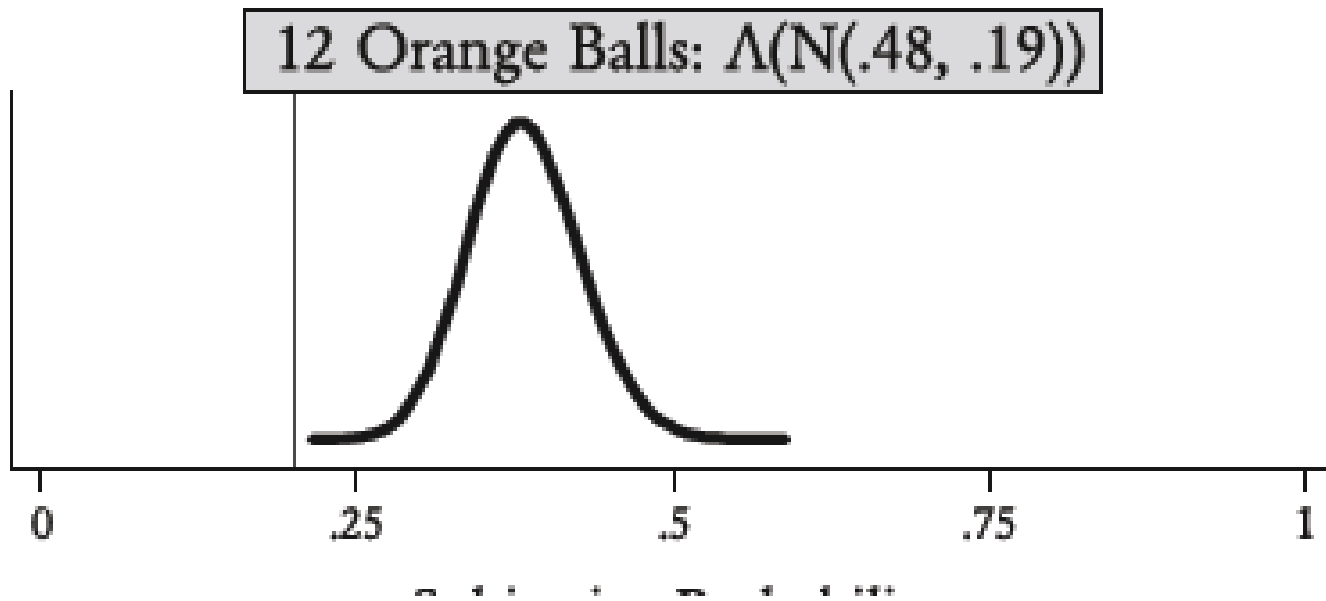
Number of orange balls out of 60	Proportion	Estimated subjective probability
6	.1	.001
12	.2	.37
30	.5	.56
33	.55	.55
45	.75	.71
48	.8	.72

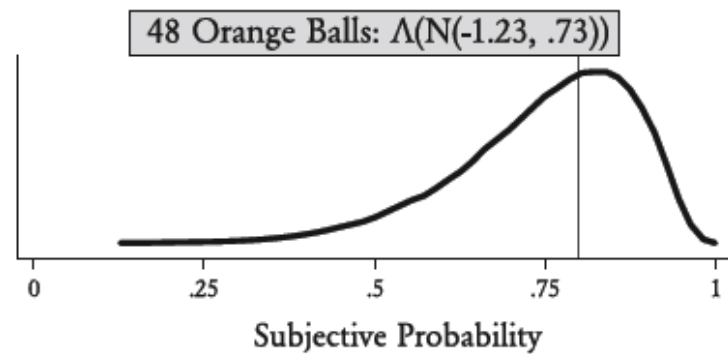
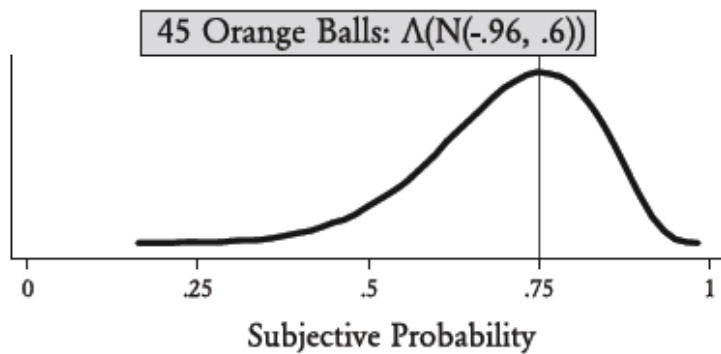
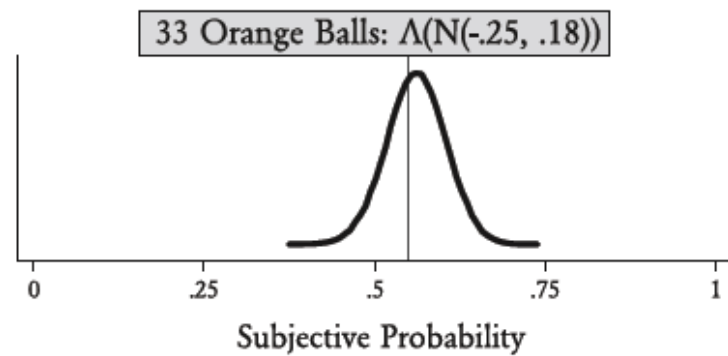
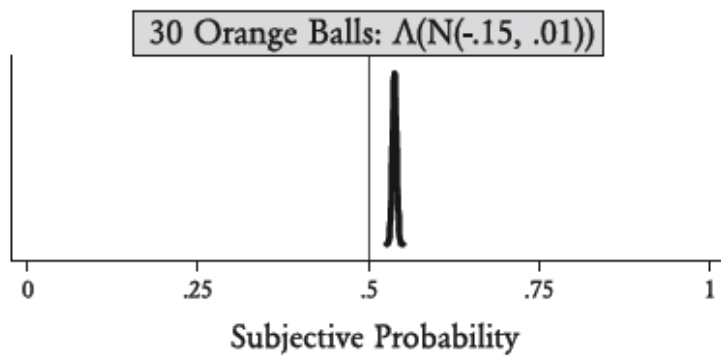
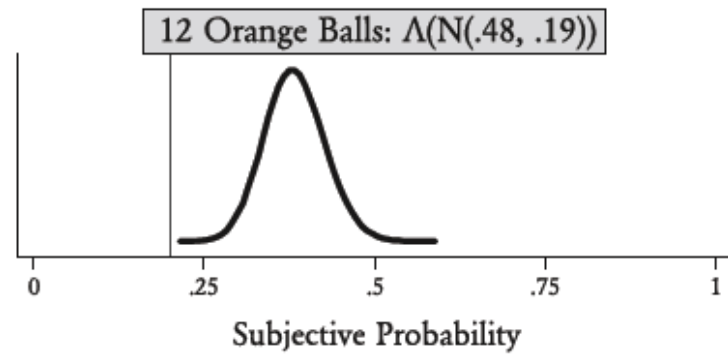
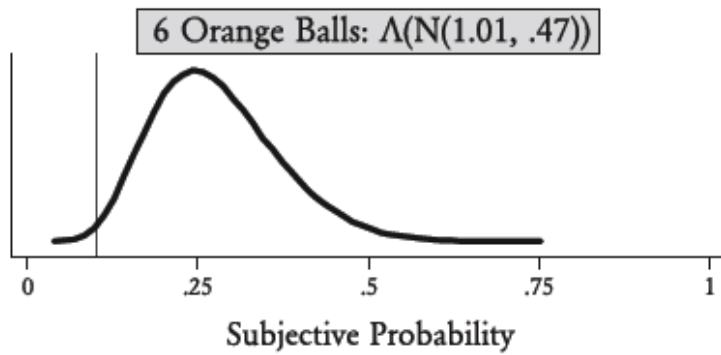
Optimism / Pessimism do not apply here  
since the outcome is neither good nor bad



# Heterogeneity

- > Estimate a (logit-normal) distribution of the probability with a mean and a standard deviation







# Conclusions

- > You should expect that demand for insurance and for risk management is heterogeneous and depend on
  - Curvatures of utility functions
  - Curvatures of probability weighting functions
  - Distributions of subjective probabilities
- > Experiments can be used to elicit these behavioral parameters
- > You cannot be casual about specifications
- > You need many tasks to elicit a full complement of parameters – it is not a quick job



# Summary of Lessons and Common Problems

- > Lesson 1: Start with theory
- > Lesson 2: You cannot implement an ideal experiment
- > Lesson 3: Details of instruments matter
- > Lesson 4: Theory needs to be augmented by a stochastic choice process
- > Lesson 5: Identification quickly becomes a problem in flexible models
- > Common Problem 1: Over fitting and under identification
- > Common Problem 2: Lack of power